Midterm Exam No. 03 (2014 Fall) PHYS 205A: University Physics

Date: 2014 Nov 5

(Name)

(Signature)

Instructions

- 1. Total time = 50 minutes.
- 2. There are 8 questions in this exam.
- 3. Equation sheet is provided separately.
- 4. To obtain partial credit for your work you need to show your work in detail and organize it clearly.

1. (10 points.) A block of mass $m = 3.00 \,\text{kg}$ is released from rest from point (A) and slides on the track shown in Figure 1. (Let $h_a = 7.00 \,\text{m}$. Do not neglect friction.) Determine the energy lost in form of frictional losses, and other forms of losses, if the block's speed at points (C) is $8.00 \,\text{m/s}$.



Figure 1: Problem 1.

2. (10 points.) A block of mass m = 10.0 kg is dropped from height h onto a spring of spring constant k = 1960 N/m. See Figure 2. If the maximum distance the spring is compressed is x = 0.20 m, find the height h.

Caution: Do not neglect the extra height the block falls due to the compression in the spring.



Figure 2: Problem 2.

3. (10 points.) The potential energy of a particle moving along the x axis is given by

$$U(x) = \left(1.0 \,\frac{J}{m^2}\right) x^2 - \left(1.0 \,\frac{J}{m^3}\right) x^3.$$
(1)

The force acting on the particle is

$$F(x) = -\frac{dU(x)}{dx}.$$
(2)

Determine the values of x at which the force is zero. (At these positions the particle is said to be in equilibrium.)

4. (10 points.) An archer weighing 60.0 kg, while standing on a frictionless surface, shoots an arrow of mass 30 grams at an angle $\theta = 60^{\circ}$ with respect to the horizontal. Determine the velocity of the archer if the arrow has been shot at 80 m/s.

5. (10 points.) Two objects, X and Y, are held at rest on a horizontal frictionless surface. A spring is compressed between X and Y. The mass of X is 3/5 times the mass of Y. When the objects are released, what is the ratio of the kinetic energy of X to that of Y? 6. (10 points.) A railroad car of mass m is moving with a speed of 3.90 m/s. It collides and couples with three other coupled railroad cars, each of the same mass as the single car and moving in the same direction with an initial speed of 1.95 m/s. What is the speed of the four cars after the collision?

7. (10 points.) A 5.0 g bullet is fired into a 2.5 kg pendulum bob initially at rest and becomes embedded in it. If the pendulum rises a vertical distance of 4.0 cm, calculate the initial speed of the bullet.

8. (10 points.) Consider a thin rod of length L placed on the positive x-axis with one end at the origin. It has a mass density (mass per length) described by

$$\lambda = a x, \tag{3}$$

where x is the distance from end placed at the origin. Here a is independent of x and is measured in grams/meter². At what distance from the end placed at the origin is the center of mass of the rod? Express your answer in terms of L.