

# Homework No. 02 (2018 Fall)

## PHYS 320: Electricity and Magnetism I

Due date: Friday, 2018 Aug 31, 2:00 PM, in class

1. **(20 points.)** Verify the following identities:

$$\nabla r = \frac{\mathbf{r}}{r} = \hat{\mathbf{r}}, \quad (1a)$$

$$\nabla \mathbf{r} = \mathbf{1}. \quad (1b)$$

Further, show that

$$\nabla \cdot \mathbf{r} = 3, \quad (2a)$$

$$\nabla \times \mathbf{r} = 0. \quad (2b)$$

Here  $r$  is the magnitude of the position vector  $\mathbf{r}$ , and  $\hat{\mathbf{r}}$  is the unit vector pointing in the direction of  $\mathbf{r}$ .

2. **(20 points.)** (Based on Problem 1.13, Griffiths 4th edition.)  
Show that

$$\nabla r^2 = 2\mathbf{r}. \quad (3)$$

Then evaluate  $\nabla r^3$ . Show that

$$\nabla \frac{1}{r} = -\frac{\hat{\mathbf{r}}}{r^2}. \quad (4)$$

Then evaluate  $\nabla(1/r^2)$ .

3. **(20 points.)** Use index notation or dyadic notation to show that

$$\nabla \times (\nabla \times \mathbf{A}) = \nabla(\nabla \cdot \mathbf{A}) - \nabla^2 \mathbf{A}, \quad (5a)$$

$$\nabla \cdot (\mathbf{A} \times \mathbf{B}) = (\nabla \times \mathbf{A}) \cdot \mathbf{B} - \mathbf{A} \cdot (\nabla \times \mathbf{B}). \quad (5b)$$